

eg. You bungee jump from 111 m using a bungee cord that is 10.0m long. If you have a mass of 85.0kg and height 2.0m (centre of mass is 1.0m)

a) what is your initial gravitational energy relative to the bottom point?

$$E_g = mgh = 85\text{kg} \times 9.8\text{N/kg} \times 111\text{m} = 92,463.0$$
$$9.25 \times 10^4 \text{ J}$$

b) what is your speed when the cord is about to start stretching?

$$mgh = \frac{1}{2} mv^2$$

$$v = \sqrt{2gh} = \sqrt{2 \times \frac{9.80\text{N}}{\text{kg}} \times 10.0\text{m}} = 19.6\text{m/s}$$

c) what elastic constant of the bungee cord will just stop you from hitting the water?

$$mgh = \frac{1}{2} kx^2$$

$$k = 2mgh/x^2 = 2(85.0\text{kg})(9.80\text{N/kg})111\text{m}$$

$$/(111\text{m}-10\text{m})^2$$

$$= 2 \times 85 \times 9.8 \times 111 / 110^2 = 15.2831$$

15.3 N/m (yes, a bit unreasonable to stretch 110m)

d) what is your acceleration at the bottom point?

$$a = F_{\text{net}}/m = (F_{\text{elastic}} - mg)/m = (kx - mg)/m$$

$$a = (15.283\text{N/m} \times 110.0\text{m} - 85.0\text{kg} \times 9.8\text{N/kg})/85.0\text{kg}$$

$$= 9.98 \text{ m/s}^2 \text{ upwards}$$

e) what is the stretch of the bungee cord at equilibrium point (where you stop bouncing)?

$$F_g = F_{\text{elastic}}$$

$$mg = kx$$

$$x = 85.0\text{kg} \times 9.80\text{N/kg} / 15.283\text{N/m}$$

$$54.5\text{m}$$

f) how much energy was lost in frictional forces when you are at rest at equilibrium point?

$$\begin{aligned}
 E_{\text{lost}} &= E_{\text{gi}} - E_{\text{elasticf}} = mgh - \frac{1}{2}kx^2 \\
 &= 85.0\text{kg}(9.80\text{N/kg})(54.5\text{m} + 10\text{m}) - \frac{1}{2} \\
 &\quad 15.283\text{N/m} (54.5\text{m})^2 \\
 &= 31\,027\text{J} = 3.10 \times 10^4\text{J lost as heat} \\
 &\quad \text{to air and cord}
 \end{aligned}$$